CHEM442-001/002
College of Charleston
Spring 2000
Exam III
1(25). Consider the $\mathrm{H}_{2}{ }^{+}$molecule-ion in which the bond length is 106 pm . A trial wave function that describes the bonding orbital is

$$
\phi(\text { bonding })=(1 / 2)^{1 / 2}\left(\Psi_{1 s A}+\Psi_{1 s B}\right)
$$

and the antibonding orbital is

$$
\phi(\text { antibonding })=(1 / 2)^{1 / 2}\left(\Psi_{1 s A}-\Psi_{1 s B}\right)
$$

where

$$
\Psi_{1 s}=(1 / \pi)^{1 / 2}\left(1 / a_{o}\right)^{3 / 2} e^{-r / a_{o}}
$$

and $a_{o}=52.92 \mathrm{pm}$. Calculate the ratio $\phi($ bonding $) / \phi($ antibonding $)$ at the position marked which lies 50 pm to the left of $\mathrm{H}_{\mathrm{A}}$.


2(25). Using the correct molecular orbital diagram for homonuclear diatomic molecules, write the complete electron configuration for $\mathrm{C}_{2}$.

Describe the bonding in the molecule and calculate the bond order.
Describe the magnetic properties of the molecule.
Using the other (incorrrect) molecular orbital diagram, write the complete electron configuration for $\mathrm{C}_{2}$. Based on this configuration, has the bond order changed? $\qquad$ Have the magnetic properties changed? $\qquad$

Returning to the correct molecular orbital diagram, write the complete electron configuration for $\mathrm{C}_{2}{ }^{-}$.

Which is more stable: $\mathrm{C}_{2}$ or $\mathrm{C}_{2}{ }^{-}$?
Which molecule has the shorter bond length ( $1.2682 \AA$ compared to $1.3117 \AA$ )? $\qquad$

For the reaction

$$
\mathrm{C}_{2}(g)+\mathrm{e}^{-} \rightarrow \mathrm{C}_{2}^{-}(g) \quad \Delta H= \pm 400 \mathrm{~kJ}
$$

which sign should appear for the enthalpy change? $\qquad$
3(25). Consider the $\mathrm{H}_{3}$ molecule in which we will assume the three nuclei to form an equilateral triangle.


Write the complete internal hamiltonian for this system listing all terms (use no summation shortcut notation).

Using simple molecular orbital theory, write a trial wave function in terms of basis functions.

Following our derivation for $\mathrm{H}_{2}{ }^{+}$and $\mathrm{H}_{2}$ in class, write the LCAO basis functions using $\Psi_{1 s}$ hydrogen-like atomic wave functions.

4(25). In laboratory we saw that only the valence electrons are important in describing the bonding in $\mathrm{H}_{2} \mathrm{O}_{2}$. Shown below are several (but not all) of the molecular orbitals drawn in scale and designated by the symmetry notation rather than $\sigma, \sigma^{*}$, etc.
$E /(\mathrm{au})$
$6 \mathrm{~A}-0.6884$
$5 \mathrm{~B}-0.2787$

| 4B | -0.4876 |
| :---: | :---: |
| 5A | -0.5038 |
| 4A | -0.5862 |
| 3B | -0.6830 |
| 3A | -0.6879 |

$2 \mathrm{~B}-\mathrm{-} .2111$
$2 \mathrm{~A}--1.4536$

How many valence atomic orbitals were used in these calculations? $\qquad$ How many molecular orbitals are generated by these calculations? $\qquad$
How many of the molecular orbitals are completely filled? $\qquad$
Sketches of three of the molecular are shown. Circle the sketch which represents $\sigma(\mathrm{OH})$ and box the sketch which represents $\sigma^{*}(\mathrm{OH})$.


