CHEM 441-02
College of Charleston
Fall 2001
Exam 2
Exam

Name $\qquad$
$1(25)$. The temperature dependence of the molar heat capacity of gaseous ethane is given by
$\left(C_{\mathrm{p}, \mathrm{m}}^{\mathrm{o}} / R\right)=(0.06436)+\left(2.137 \times 10^{-2} \mathrm{~K}^{-1}\right) T-\left(8.263 \times 10^{-6} \mathrm{~K}^{-2}\right) T^{2}+\left(1.024 \times 10^{-9} \mathrm{~K}^{-3}\right) T^{3}$
A one-molar sample of ethane at $25^{\circ} \mathrm{C}$ is isobarically heated to 1000 K by placing it in an oven at 1500 K . Calculate
a) $q$
b) $w$
c) $\Delta H$
d) $\Delta U$
e) $\Delta S$ (system $)$
f) $\Delta S$ (surroundings)
g) $\Delta S$ (universe)

2(25). The volume of the ethane sample in the first question is isothermally and reversibly decreased from 250 L to 100 L at 1000 K . Calculate
a) $q$
b) $w$
c) $\Delta H$
d) $\Delta U$
$\begin{array}{lll}\text { e) } \Delta S(\text { system }) & \text { f) } \Delta S(\text { surroundings }) & \text { g) } \Delta S \text { (universe) }\end{array}$

3(25). Use the thermochemical information at 298 K provided
$\begin{array}{ll}1 / 2 \mathrm{H}_{2}(\mathrm{~g})+1 / 2 \mathrm{~F}_{2}(\mathrm{~g}) \rightarrow \mathrm{HF}(\mathrm{g}) & \Delta_{\mathrm{r}} H=-273.3 \mathrm{~kJ} \\ \mathrm{H}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) & \Delta_{\mathrm{r}} H=-285.8 \mathrm{~kJ}\end{array}$
$S /\left(\mathrm{J} \mathrm{K}^{-1} \mathrm{~mol}^{-1}\right)=130.684$ for $\mathrm{H}_{2}(\mathrm{~g}), 202.78$ for $\mathrm{F}_{2}(\mathrm{~g}), 173.779$ for $\mathrm{HF}(\mathrm{g}), 205.138$ for $\mathrm{O}_{2}(\mathrm{~g}), 69.91$ for $\mathrm{H}_{2} \mathrm{O}(\mathrm{l})$
to calculate $\Delta_{\mathrm{r}} H$ and $\Delta_{\mathrm{r}} S$ for
$2 \mathrm{~F}_{2}(\mathrm{~g})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightarrow 4 \mathrm{HF}(\mathrm{g})+\mathrm{O}_{2}(\mathrm{~g})$
4(20). We know that for nonmetals $\Delta S=C_{\mathrm{p}} / 3$ from $T=0$ to the lowest temperature at which a $C_{\mathrm{p}}$ value is given. For a metal at very low temperature, the heat capacity consists of two contributions
$C_{\mathrm{p}}=\alpha T^{3}+\gamma T$
Derive a similar expression for $\Delta S$ from $T=0$ to the lowest temperature at which a $C_{\mathrm{p}}$ value is given.
$5(15)$. Consider an ensemble of 1000 isolated systems (same energy $E$, volume $V$, and number of particles, $N$ ). The number of ways of having $a_{1}$ systems in state $1, a_{2}$ systems in state 2 , etc. is $W=A!/ a_{1}!a_{2}!\cdots$. Calculate the maximum value of $W$ for a simple ensemble consisting of 4 states. (Hint: logarithms)

5(15). For pyradine

| $T /(\mathrm{K})$ | 13.08 | 21.26 | 28.53 | 35.36 | 48.14 | 64.01 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $C_{\mathrm{p}}\left(\mathrm{cal} \mathrm{K}^{-1} \mathrm{~mol}^{-1}\right)$ | 1.063 | 2.888 | 4.610 | 6.049 | 8.060 | 9.739 |


| 82.91 | 101.39 | 119.37 | 132.32 | 151.57 | 167.60 | 179.44 | 193.02 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 11.093 | 12.156 | 13.175 | 13.940 | 15.161 | 16.265 | 17.150 | 18.276 |


| 201.61 | 212.16 | 223.74 | 239.70 | 254.41 | 273.75 | 293.93 | 307.16 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 19.081 | 20.183 | 22.545 | 29.213 | 29.765 | 30.575 | 31.521 | 32.159 |

$S_{10}=0.166 \mathrm{cal} \mathrm{K}^{-1} \mathrm{~mol}^{-1}$
$\Delta_{\text {fus }} H=1978 \mathrm{cal} \mathrm{mol}^{-1}$ at 231.49 K
Explain in detail how to find $S_{298}$.

